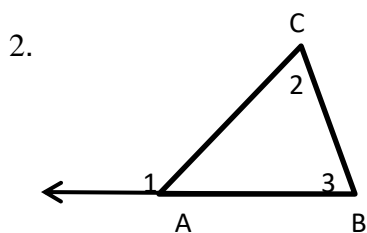


Segment and Angle Relationships – Intro to Geometry

| By Angle | By Sides |
|----------------------|-------------|
| Acute | Scalene |
| Obtuse | Isosceles |
| Right | Equilateral |
| Equiangular | |
| Triangle Sum Theorem | |

| |
|-----------------------|
| Midpoint of a Segment |
| Bisect |
| Vertical Angles |
| Linear Pair |
| Complementary |
| Supplementary |

1. What does the sum of the measures of the angle of a triangle equal?



a. Find $m\angle 1 + m\angle CAB$ _____

b. Find $m\angle 2 + m\angle 3 + m\angle CAB$ _____

c. Using parts a and b, what do you know about $m\angle 1$ and $m\angle 2 + m\angle 3$?

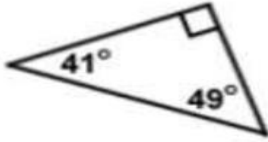
3.

a. Write the Pythagorean Theorem: _____

b. With what kind of triangle can you use the Pythagorean Theorem? _____

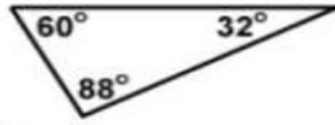
4. Classify each triangle as acute, right or obtuse:

a)



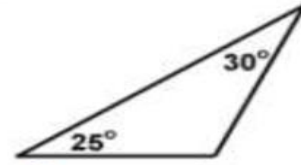
a) _____

b)



b) _____

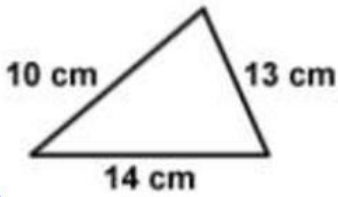
c)



c) _____

5. Classify each triangle as scalene, isosceles, or equilateral.

a)



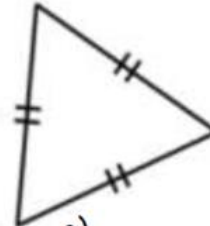
a) _____

b)



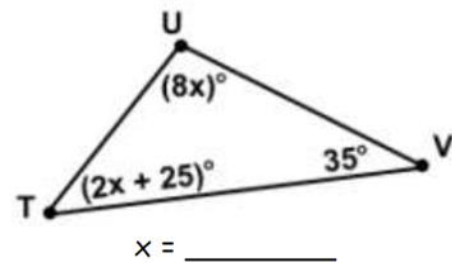
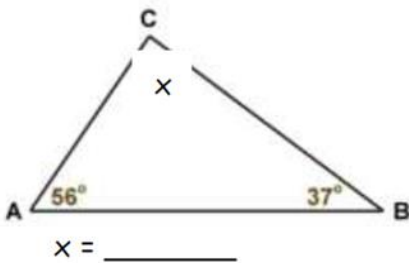
b) _____

c)

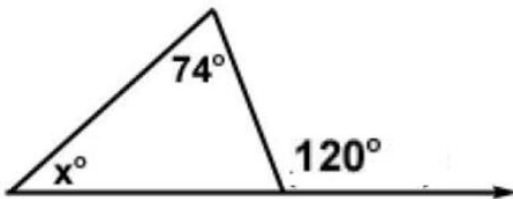


c) _____

6. Solve for x in each triangle:

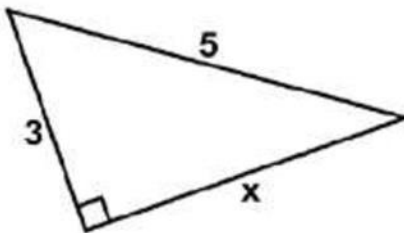


7. Solve for x:

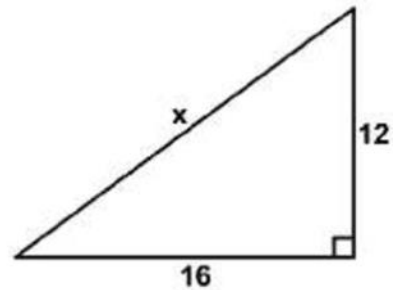


$x = \underline{\hspace{2cm}}$

8. Solve using Pythagorean Theorem



$x = \underline{\hspace{2cm}}$



$x = \underline{\hspace{2cm}}$

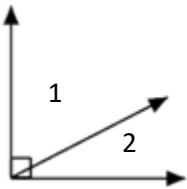
For each problem: a) Draw and label a picture, b) Write an equation, and c) Solve for x.

9. If C is the midpoint of \overline{AB} , AC is $2x + 1$, CB is $3x - 4$, find x



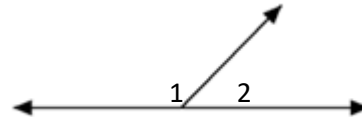
10. If T is the midpoint of \overline{PQ} , $PT = 5x + 3$, $TQ = 7x - 9$, find x.

11. $m\angle 1 = 4x - 3$ and $m\angle 2 = x + 8$. Find x and $m\angle 2$.



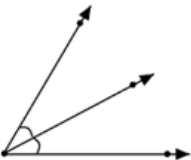
12. $\angle 5$ and $\angle 6$ are complementary. If $m\angle 5 = 8x - 6$ and $m\angle 6 = 14x + 8$, find x.

13. $m\angle 1 = 2x + 4$ and $m\angle 2 = 6x + 20$. Find x



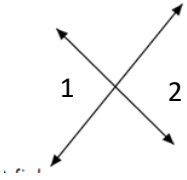
14. $\angle 3$ and $\angle 4$ are supplementary. $m\angle 3 = 12x - 15$ and $m\angle 4 = 3x + 45$. Find x

15. If \overrightarrow{BX} bisects $\angle ABC$, $m\angle ABX$ is $5x$ and $\angle XBC = 3x + 10$, find x.



16. If \overrightarrow{KN} bisects $\angle JKL$, $m\angle JKN = 4x - 16$ and $m\angle NKL = 2x + 6$, find x.

17. If $m\angle 1 = x + 10$ and $m\angle 2 = 4x - 35$. Find x .

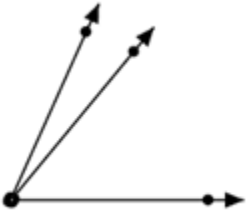


18. $\angle 3$ and $\angle 4$ are vertical angles. $m\angle 3 = 3x + 8$ and $m\angle 4 = 5x - 20$, find x .

19. Point S is between points D and T. If $DT = 60$, $DS = 2x - 8$, and $ST = 3x - 12$, find x .

20. Point F is between points E and G. If $EF = 4x - 20$, $FG = 2x + 30$, and $EG = 100$, find x .

21. $m\angle ADC$ is $5x - 20$, $m\angle ADB = x - 4$, $m\angle BDC = x + 5$. Find x .



Honors Examples:

1. A is between B and C. $BA = x^2$, $AC = 6x + 10$, and $BC = 17$. Find x and the length of each segment.

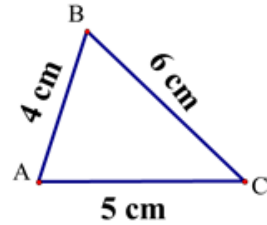
2. L is between K and M. $KL = x^2 - 10$, $LM = 5x + 4$, and $KM = 2x^2 - 42$. Find x .

Triangle Inequalities:

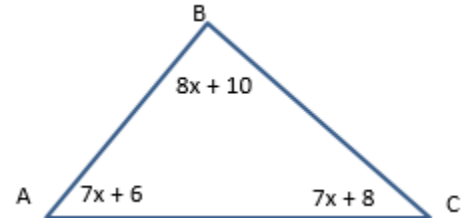
Triangle Set Up

***You should already know this:

- The smallest side is across from the smallest angle.
- The largest side is across from the largest side



Ex: List the sides in order from shortest to longest measure:



Triangle Inequality Theorem:

The sum of the lengths of any two sides of a triangle is greater than the length of the third side.

Ex: Determine if it is possible to draw a triangle with side measures 12, 11, 17.

Practice:

Can you draw a triangle using these lengths for the sides?

| | | | |
|------------|------------|-------------------|-------------|
| 1. 5, 7, 9 | 2. 3, 4, 1 | 3. 5.2, 5.5, 10.1 | 4. 7, 7, 14 |
|------------|------------|-------------------|-------------|

Finding the range of the third side given two sides:

- The 3rd side cannot be larger than the other two added together.

○ _____

- The sum of the 3rd side and the smallest side cannot be larger than the other side

○ _____

Ex: Given a triangle with sides of length 3 and 8, find the range of possible values for the third side.

Practice:

Given the 1st two sides, give the range for the 3rd side of an inequality.

| | | |
|--------------|--------------|------------|
| 1. 15 and 20 | 2. 22 and 34 | 3. 9 and 8 |
|--------------|--------------|------------|

Practice

For each set of lengths, determine whether it is possible to draw a triangle with sides of the given measures. If possible, write yes. If not possible, write no.

1. 3, 4, 5 _____ 2. 4, 9, 5 _____ 3. 5, 6, 12 _____

4. 7, 3.5, 4.5 _____ 5. 4, 5, 8.5 _____ 6. .5, 1.2, .6 _____

The lengths of two sides of a triangle are given. Find the two numbers that the third side must fall between.

7. 3 and 8 _____ $< x <$ _____

8. 12 and 25 _____ $< x <$ _____

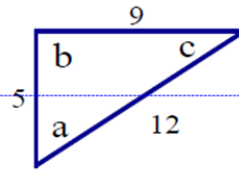
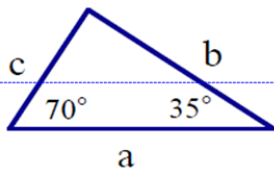
9. 13 and 4 _____ $< x <$ _____

10. 13 and 21 _____ $< x <$ _____

Arrange the letters in order from greatest to least.

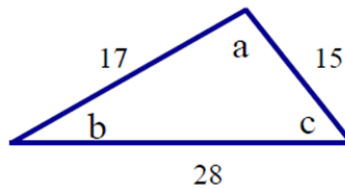
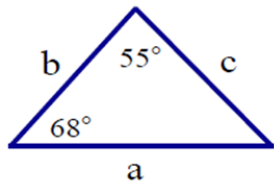
11. _____ $>$ _____ $>$ _____

12. _____ $>$ _____ $>$ _____



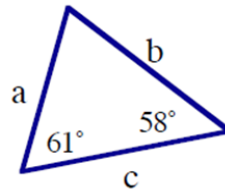
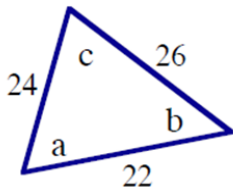
13. _____ $>$ _____ $>$ _____

14. _____ $>$ _____ $>$ _____



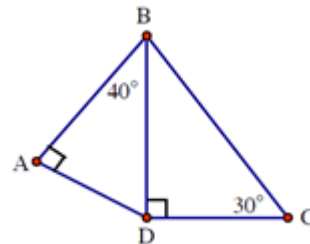
15. _____ $>$ _____ $>$ _____

16. What conclusion can we draw from this triangle?



4. Name the shortest segment. _____

5. Name the longest segment. _____

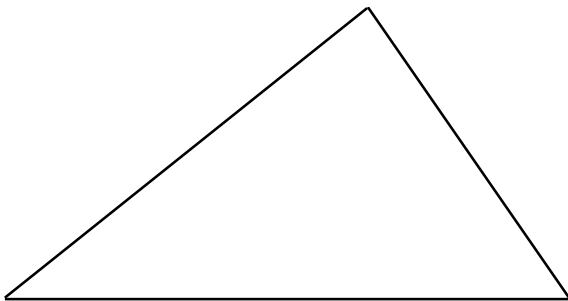


Special Segments in Triangles:

Altitudes, Medians, Angle Bisectors & Perpendicular Bisectors

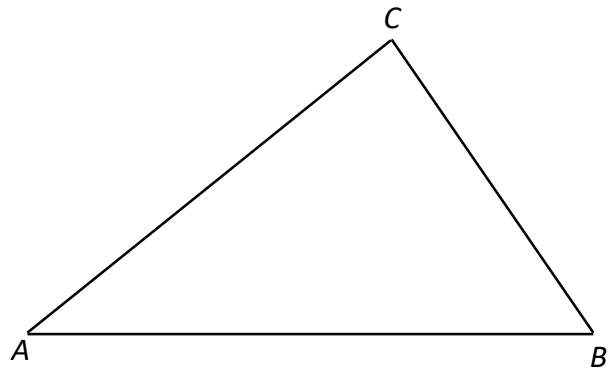
What is a median?

Measure the lengths of each side and sketch all three medians in the triangle below.



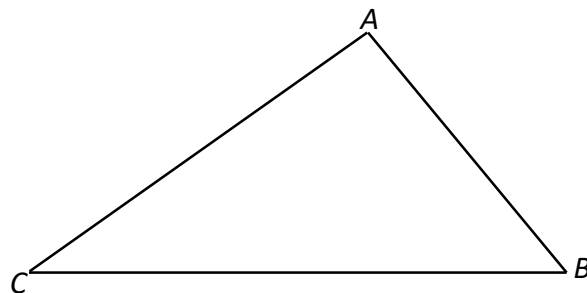
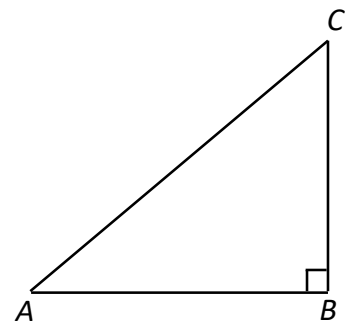
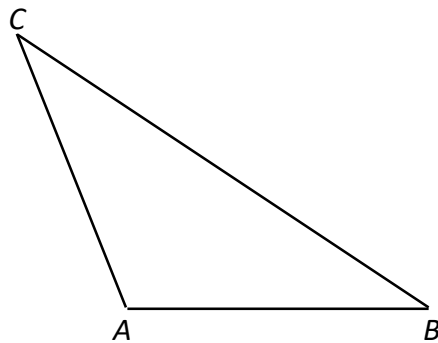
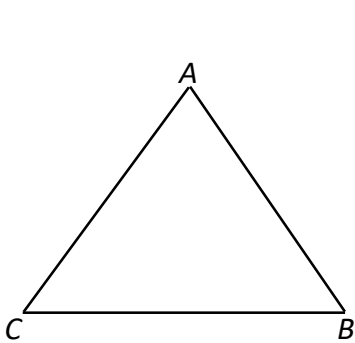
What is an angle bisector?

Sketch angle bisector \overline{CD} .



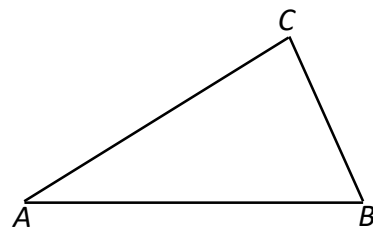
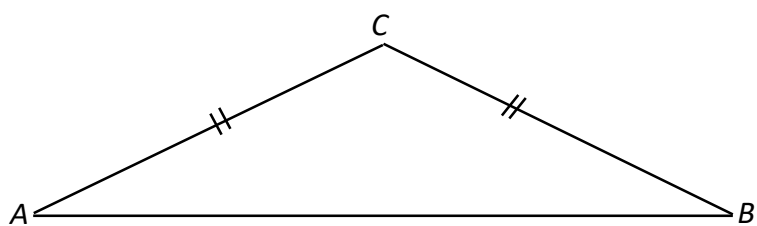
What is an altitude?

Sketch an altitude from vertex C to \overline{AB} in each triangle below.



What is a perpendicular bisector?

Sketch the perpendicular bisector of \overline{AB} in the triangles below.



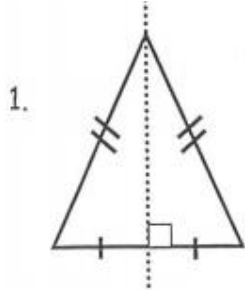
| ORGANIZER | Through Vertex | Through Midpoint | Forms right angle | Picture |
|------------------------|----------------|------------------|-------------------|---------|
| Median | | | | |
| Altitude | | | | |
| Perpendicular Bisector | | | | |
| Angle Bisector | | | | |
| Midsegment | | | | |

Example: Sketch a picture of each statement.

| | |
|---|---|
| a) \overline{AD} is an altitude of $\triangle ABC$ | b) \overline{AD} is a median of $\triangle ABC$ |
| c) \overline{DE} is a perpendicular bisector of $\triangle ABC$. E is between B and C. | |

Examples: Determine which special segment is shown for each

1. _____



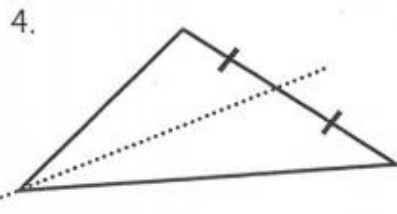
2. _____

2.

3.

3. _____

4. _____



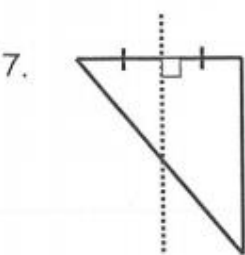
5.

6.

5. _____

6. _____

7. _____



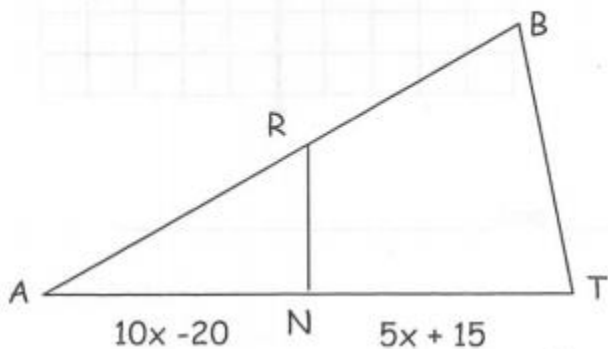
8.

9.

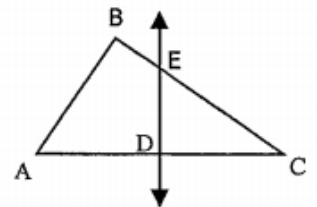
8. _____

9. _____

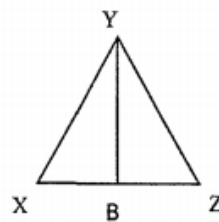
RN is the perpendicular bisector of AT. How would you find the value of x?
What are the lengths of AN and NT?



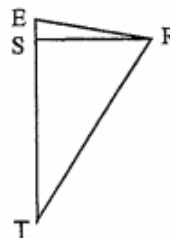
6) In $\triangle ABC$, \overline{DE} is perpendicular bisector of \overline{AC} with D on \overline{AC} . If $AD = 2y + 4$, $CD = y + 12$, and $m\angle EDC = 5(x - 12)^\circ$. Find the value of x and y. Find length of AD , DC , and AC .



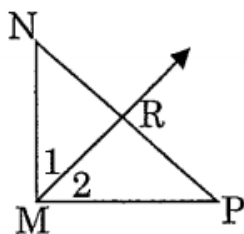
9) \overline{YB} is an altitude of $\triangle XYZ$, and $m\angle YBZ = (6x - 6)^\circ$. Find the value of x . What is the measure of $\angle YBZ$?



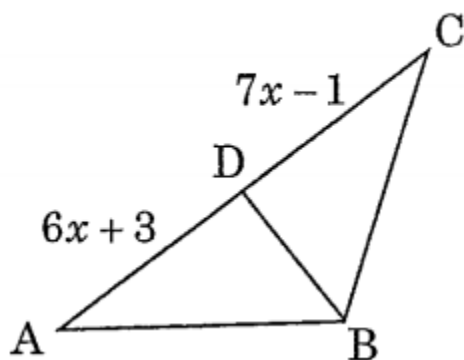
\overline{RS} is an altitude of $\triangle RTE$, $m\angle SRT = (4x - 8)^\circ$, and $m\angle STR = (6x + 13)^\circ$. Find the value of x .



2) \overline{MR} is the angle bisector of $\angle NMP$. Find x if $m\angle 1 = 5x + 8$ and $m\angle 2 = 8x - 16$.

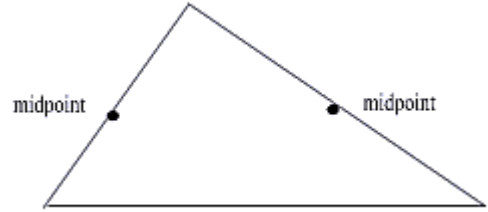


6) \overline{BD} is a median. Find the x

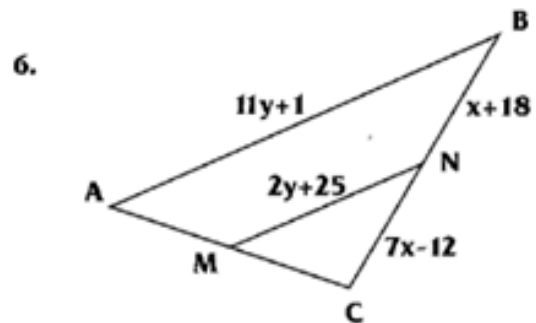
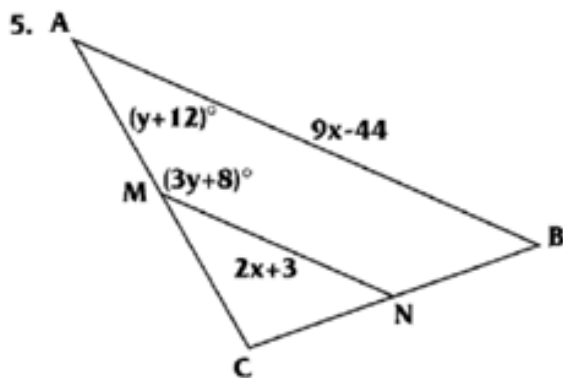
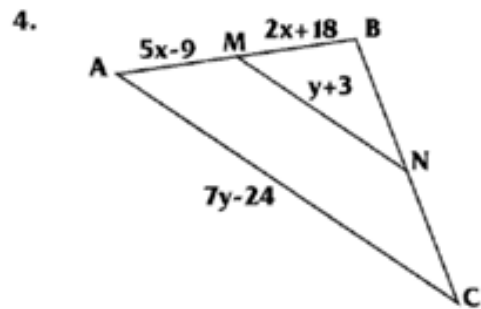
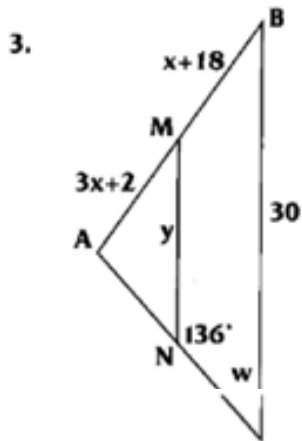
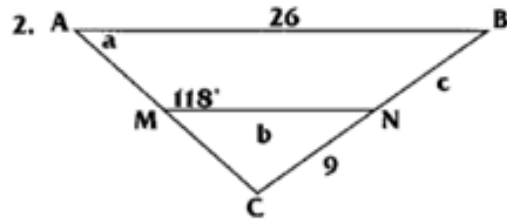
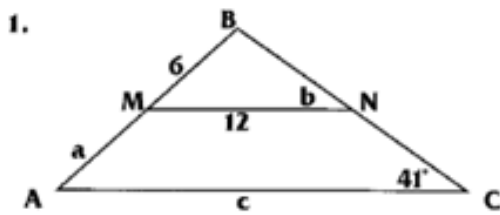
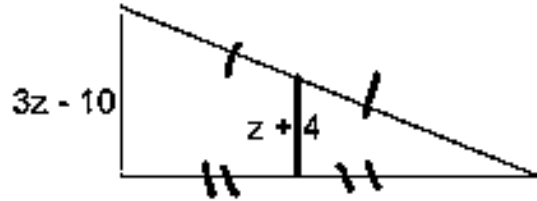
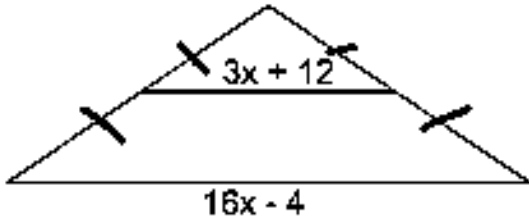


Mid-Segment, Isosceles Triangle Theorem, and Exterior Angle Theorem

Mid-segment – _____

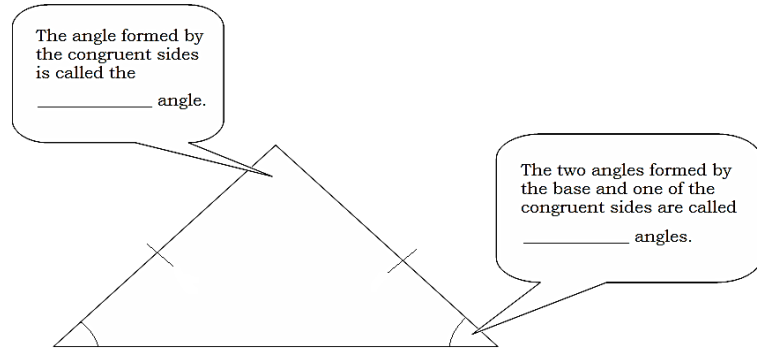


Examples:

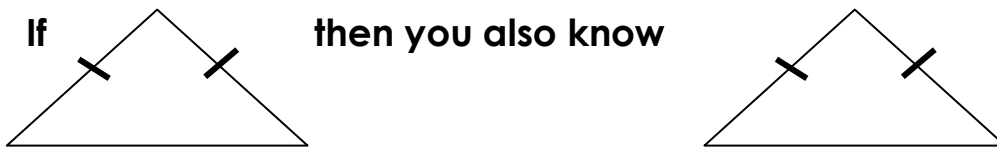


Isosceles Triangle: A triangle with 2 sides congruent sides.

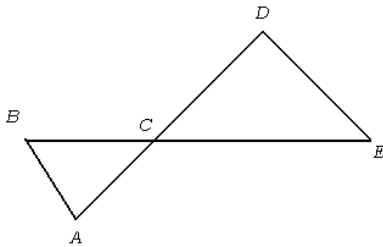
Example #1: label $\triangle ABC$ as isosceles with $\angle C$ as the vertex angle. Find x and the measure of each side if $BC = 2x + 4$, $BD = x + 2$ and $CD = 10$.



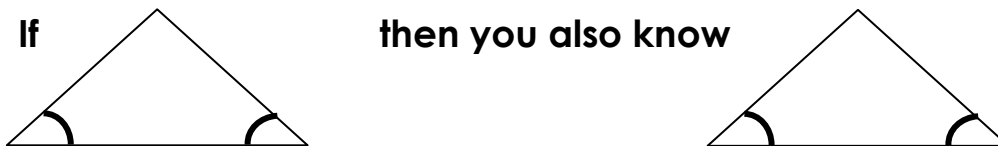
Isosceles Triangle Theorem: If two sides of a triangle are congruent, then the angles opposite those angles are congruent



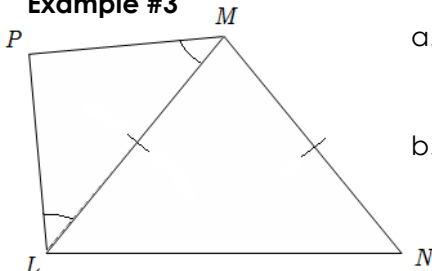
Example #2: If $\overline{DE} \cong \overline{CD}$, $\overline{BC} \cong \overline{AC}$, and $m\angle CDE = 120$, what is the measure of $\angle BAC$?



Theorem: If two angles of a triangle are congruent, then the sides opposite those angles are congruent



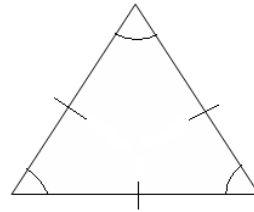
Example #3



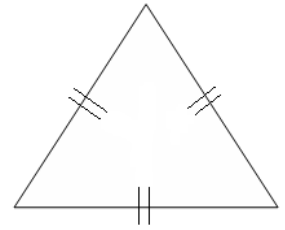
a.) Name all of the congruent angles.

b.) Name all of the congruent segments.

Corollary: A triangle is equilateral if and only if it is equiangular.



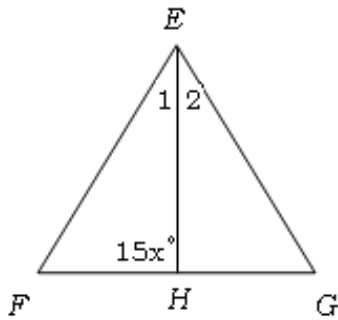
Corollary: Each angle of an equilateral triangle measures



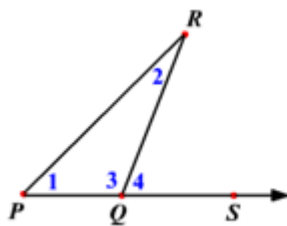
Example #4: $\triangle EFG$ is equilateral, and \overline{EH} bisects $\angle E$.

a.) Find $m\angle 1$ and $m\angle 2$.

b.) Find x .



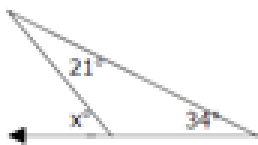
Exterior Angle Theorem :



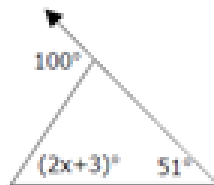
$$m\angle 4 = m\angle 1 + m\angle 2$$

Solve for x :

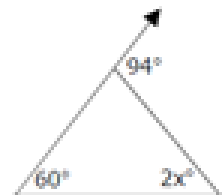
1. $x =$ _____



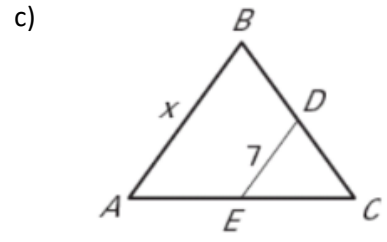
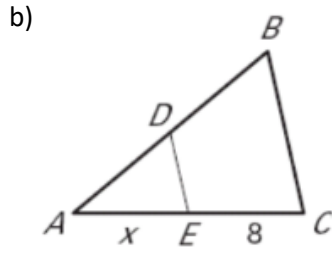
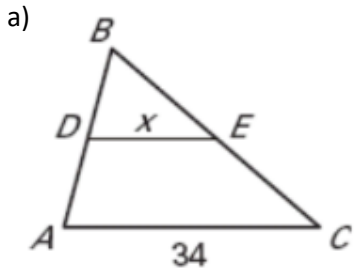
2. $x =$ _____



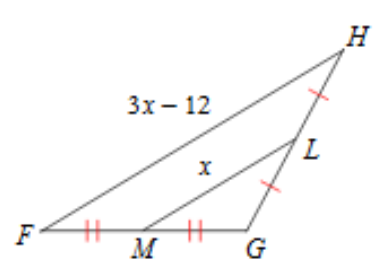
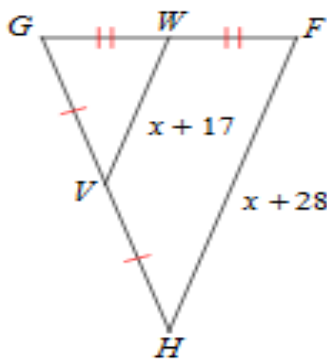
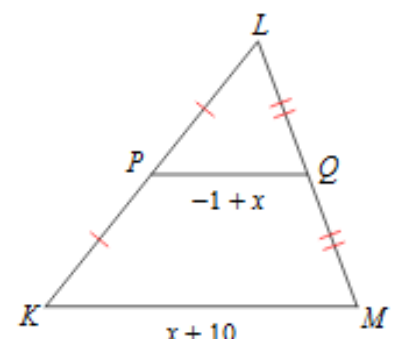
3. $x =$ _____



Example 1: \overline{DE} is a midsegment of $\triangle ABC$. Find the value of x .

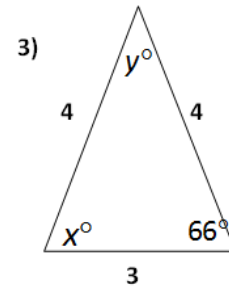
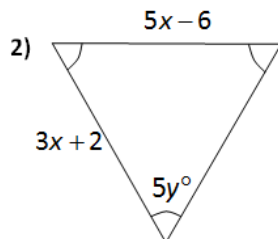
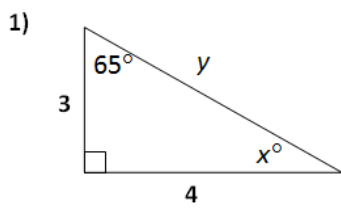


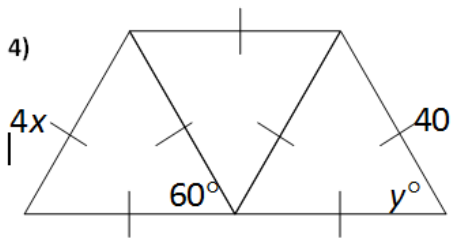
Examples:

| | | |
|---|--|--|
| <p>1) </p> | <p>2) </p> | <p>3) </p> |
|---|--|--|

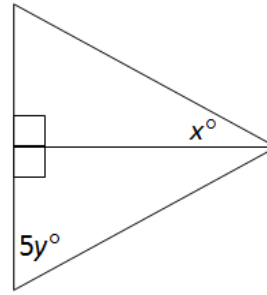
Find the value of x and y .

Find the value of x and y

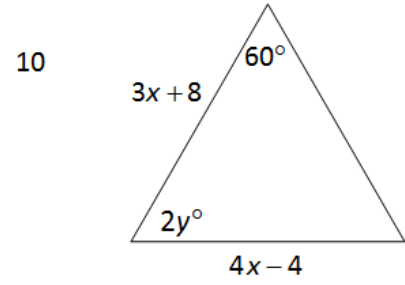




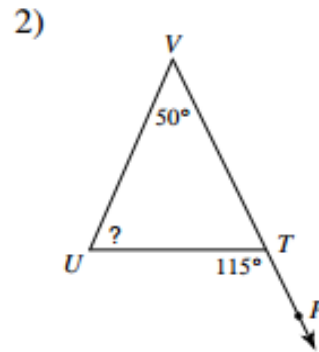
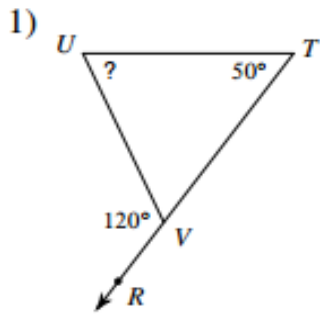
5) Equilateral Triangle



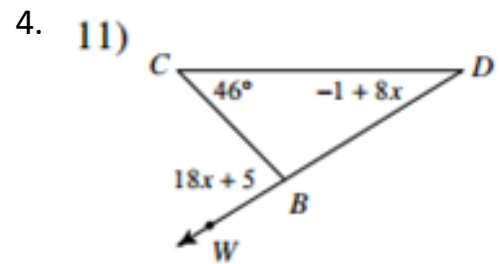
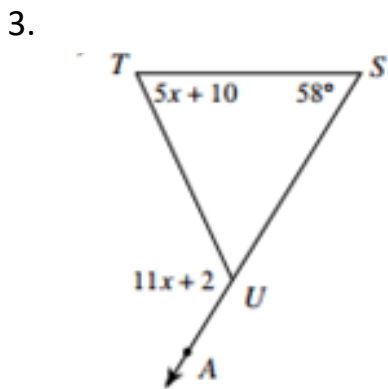
6) Equilateral Triangle



Find the measure of each angle indicated.



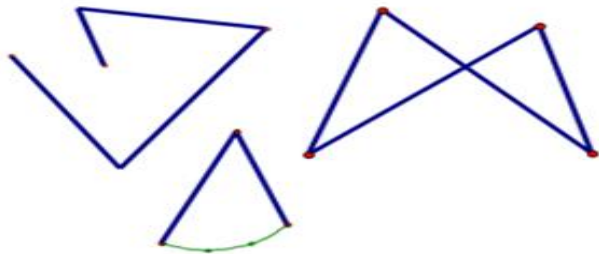
Solve for x.



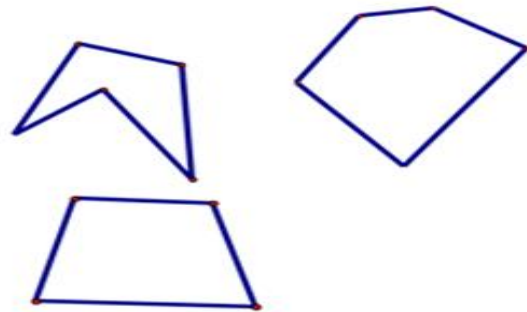
Polygons

Definitions:

A closed figure formed by a finite number of coplanar segments so that each segment intersects exactly two others, but only at their endpoints.

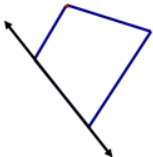
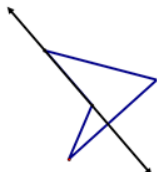
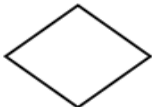



These figures are **not polygons**



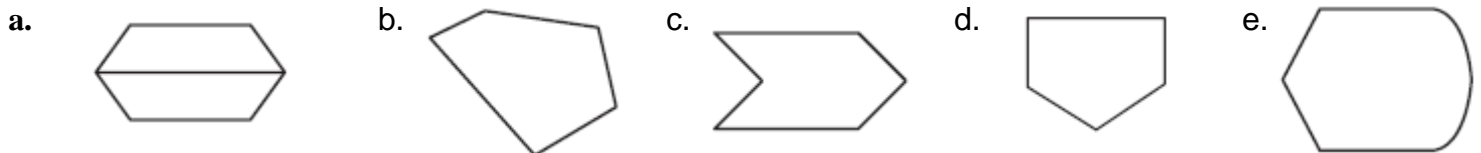
These figures are **polygons**

Classification of Polygon

| | | | |
|---|--|--|---|
| <p>Convex: does NOT cave in on itself</p>  | <p>Concave: does cave in on itself</p>  | <p>Regular: A convex polygon in which all interior angles have the same measure and all sides are the same length</p>  | <p>Irregular: Two sides (or two interior angles) are not congruent.</p>  |
|---|--|--|---|

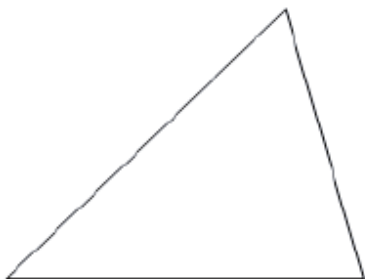
Identify polygons

Tell whether the figure is a polygon and whether it is a concave polygon, convex polygon, or not a polygon.



| # of Sides | Name of Poly | # of Sides | Name of Poly | # of Sides | Name of Poly |
|------------|--------------|------------|--------------|------------|--------------|
| 3 | | 6 | | 9 | |
| 4 | | 7 | | 10 | |
| 5 | | 8 | | 12 | |

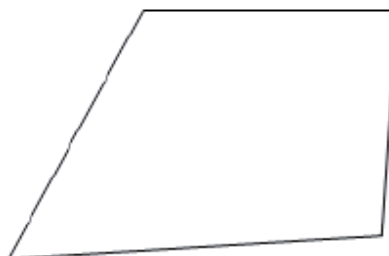
From one vertex in each polygon, draw diagonals to the nonconsecutive vertices. Use the triangles to find the sum of the interior angles of each polygon.



#sides= _____

#triangles= _____

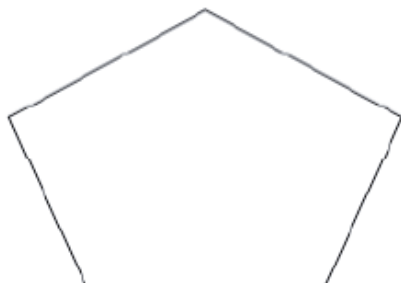
sum of interior angles= _____



#sides= _____

#triangles= _____

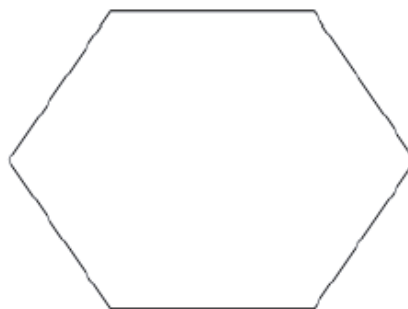
sum of interior angles= _____



#sides= _____

#triangles= _____

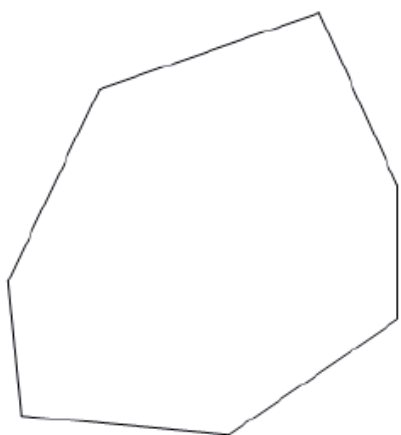
sum of interior angles= _____



#sides= _____

#triangles= _____

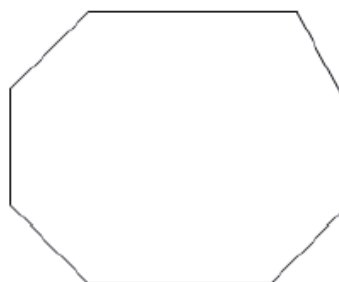
sum of interior angles= _____



#sides= _____

#triangles= _____

sum of interior angles= _____



#sides= _____

#triangles= _____

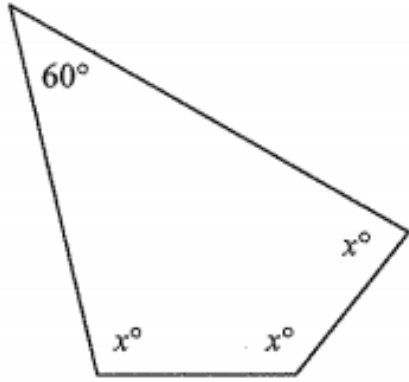
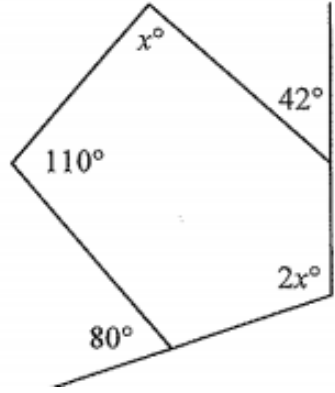
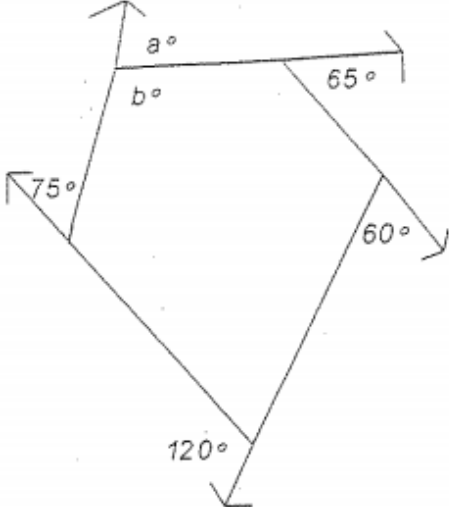
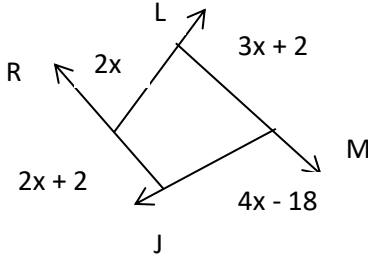
sum of interior angles= _____

| POLYGON NAME | # of SIDES | # of TRIANGLES | SUM OF INT \angle 'S | EACH INT \angle (regular) | SUM OF EXT \angle 'S | EACH EXT \angle (regular) |
|---------------|------------|----------------|------------------------|-----------------------------|------------------------|-----------------------------|
| TRIANGLE | | | | | | |
| QUADRILATERAL | | | | | | |
| PENTAGON | | | | | | |
| HEXAGON | | | | | | |
| HEPTAGON | | | | | | |
| OCTAGON | | | | | | |
| NONAGON | | | | | | |
| DECAGON | | | | | | |
| DODECAGON | | | | | | |
| n-gon | | | | | | |

Summary of Convex Polygon Formulas:

| Sum of Interior Angles | Measure of ONE Interior Angle | Sum of Exterior Angles | Measure of ONE Exterior Angle |
|------------------------|-------------------------------|------------------------|-------------------------------|
| | | | |

Examples:

| | |
|---|--|
| <p>1. Sum of the measures of the interior angles of a 11-gon is</p> | <p>2. The measures of an exterior angle of a regular octagon is</p> |
| <p>3. The number of sides of a regular polygon with exterior angles 72° is</p> | <p>4. The measure of an interior angle of a regular polygon with 30 sides</p> |
| <p>5. Find x.</p>  | <p>6. Find x.</p>  |
| <p>7. Find a and b.</p>  | <p>8. Find the measure of $\angle RKL$.</p>  <p>A. 34° B. 68° C. 86° D. 148°</p> |

